

# Comparing Walk-In, Open Access, and Traditional Appointment Scheduling in Outpatient Health Care Clinics

1

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# Agenda

2

1. Problem Setting
2. Open Access and Walk-in Models
3. Computational Results
4. Managerial Implications
5. Future Research and Conclusions

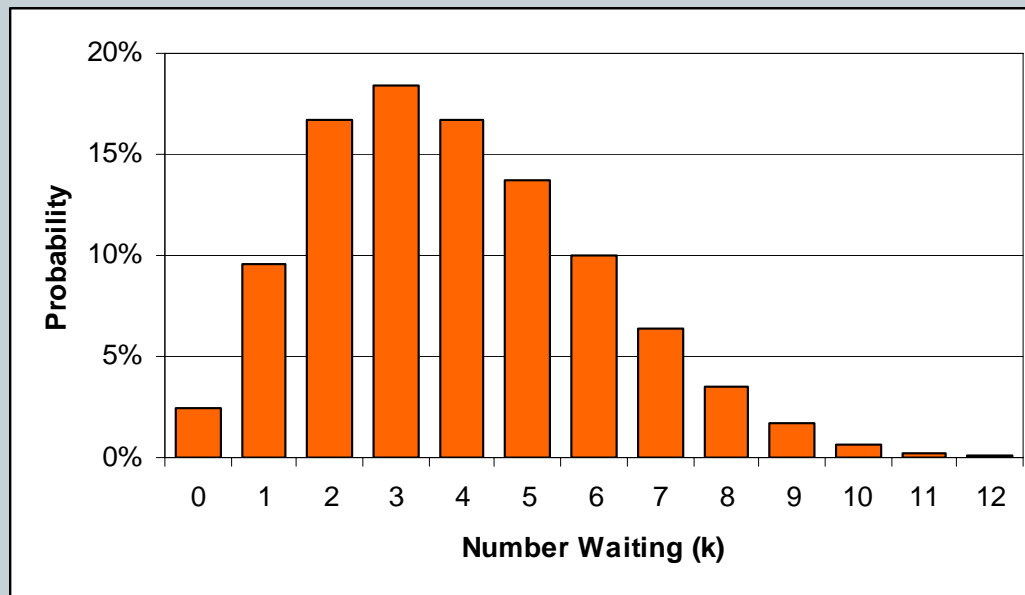
# Objectives of Research

3

- **Optimize patient flow in health-care clinics**
  - Traditionally scheduled (TS) clinic
    - ✦ Some patients do not “show” for scheduled appointments
  - TS clinic wishes to increase scheduling flexibility
    - ✦ Some capacity allocated to “open access” (OA) appointments, OR
    - ✦ Some capacity allocated to “walk-in” traffic
  - Balance needs of clinic, providers, and patients
- **Study impact of open access and walk-in traffic**
  - When is open access or walk-in traffic beneficial?
  - What mix of TS, OA, and WI traffic is best?
  - What are trade-offs of TS, OA, and WI on clinic performance?

# 2. Appointment Scheduling Model

4



# Assumptions

5

- A clinic session has  $N$  treatment slots
  - Each slot is  $d$  time units long (deterministic)
  - A clinic session then is  $D=Nd$  time units in duration
- One or multiple undifferentiated providers  $P$ 
  - Clients serviced by any available provider
- Patients can arrive in one of three ways
  - Binomial traditional appointments “show” with probability  $\sigma$
  - Poisson open access call-ins with mean  $\varphi$  (per day)
  - Poisson walk-ins with mean  $\lambda$  (per appointment slot)
  - Arrivals have equal service priority (undifferentiated)

# Characteristics of Model

6

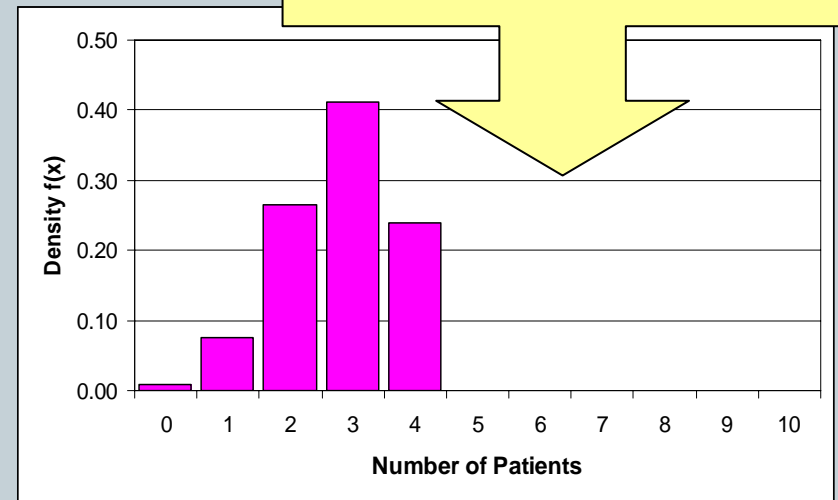
- **Model flexibility**
  - Appt show rates  $\sigma_j$  can vary by treatment slot  $j$  (time of day)
  - Open access call-in rate  $\varphi$  can vary by day.
  - Walk-in rate  $\lambda_j$  can vary by treatment slot  $j$
  - Number of providers  $P_j$  can vary by slot  $j$
  - Any arrival distribution can be accommodated
- **Patient arrivals**
  - Patients are only seen at the start of a treatment slot (early arrivals wait for next slot without cost)
  - Patients are seen in order of arrival (FCFS)

# Arrival of Scheduled Appointments

7

- Appointment arrivals are binomially distributed
  - $s_j$  patients scheduled for treatment slot  $j$
  - Probability of a patient showing is  $\sigma$
  - $a_j \leq s_j$  actually arrive in slot  $j$

Binomial distribution has no right tail



$$s_j = 4, \sigma = 70\%$$

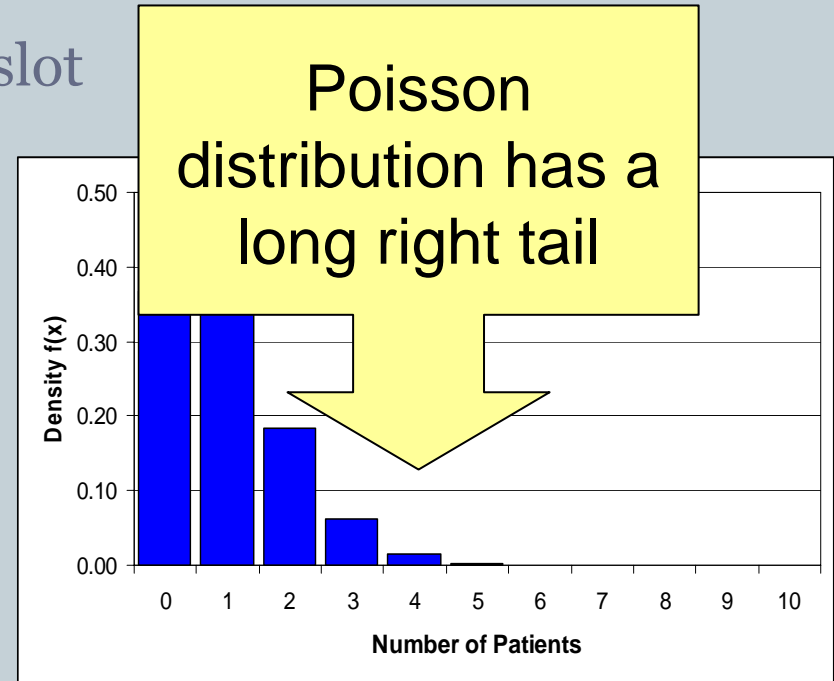
$$b(a_j; s_j, \sigma) = \binom{s_j}{a_j} \sigma^{a_j} (1-\sigma)^{s_j-a_j}$$

# Arrival of Walk-In Patients

8

- Walk-ins arrive at some percentage of clinic capacity
- Walk-in arrivals are Poisson distributed
  - Walk-ins arrive at rate  $\lambda$  per slot
  - $w_j$  actually walk-in in slot  $j$

$$p(w_j; \lambda) = \frac{\lambda^k e^{-\lambda}}{w_j!}$$



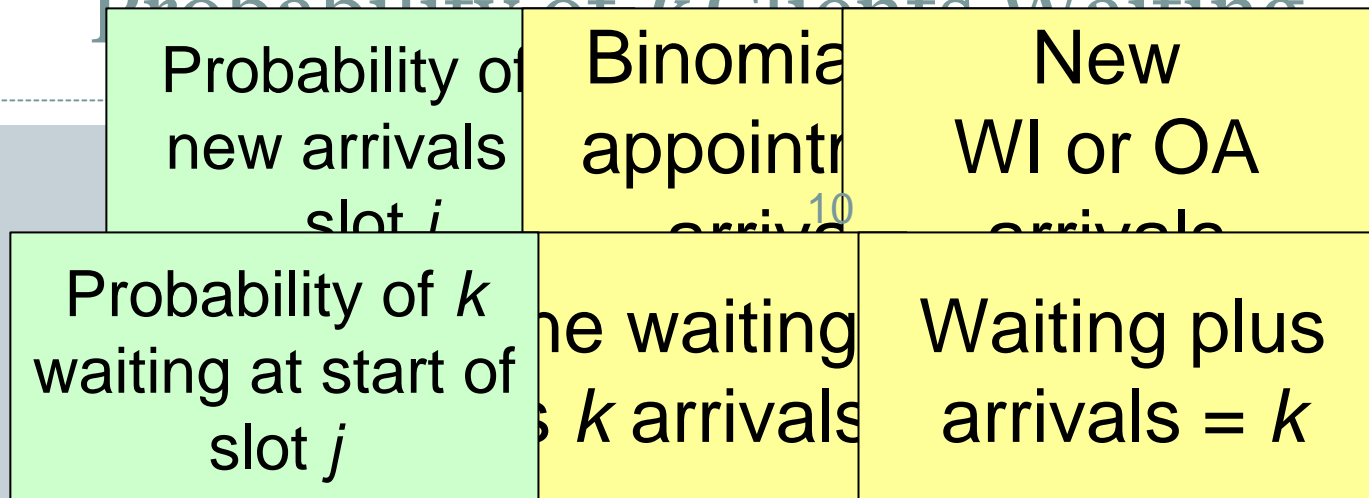
$$\lambda = 1$$

# Arrival of Open Access Patients

9

- Open access (OA) calls arrive at a mean rate equal to some fraction of clinic capacity (e.g., 50%)
- Patients call for a same-day appointment
  - Number of OA patients calling on a particular day is Poisson distributed with mean  $\varphi$
  - “Turned away” if no open slots remain that day
    - ✦ Perhaps make an appointment on another day
    - ✦ OA patients always show for appointments

# Probability of $k$ Clients Waiting



$$\theta_{j+1,k} = \theta_{j,0} \alpha_{j+1,k} + \sum_{i=0}^k \theta_{j,i+1} \alpha_{j+1,k-i}$$

- $\alpha_{jk}$  = probability of  $k$  clients arriving for service at the start of appointment slot  $j$
- $\theta_{jk}$  = probability of  $k$  clients waiting for service at start of appointment slot  $j$

# Relative Benefits and Penalties

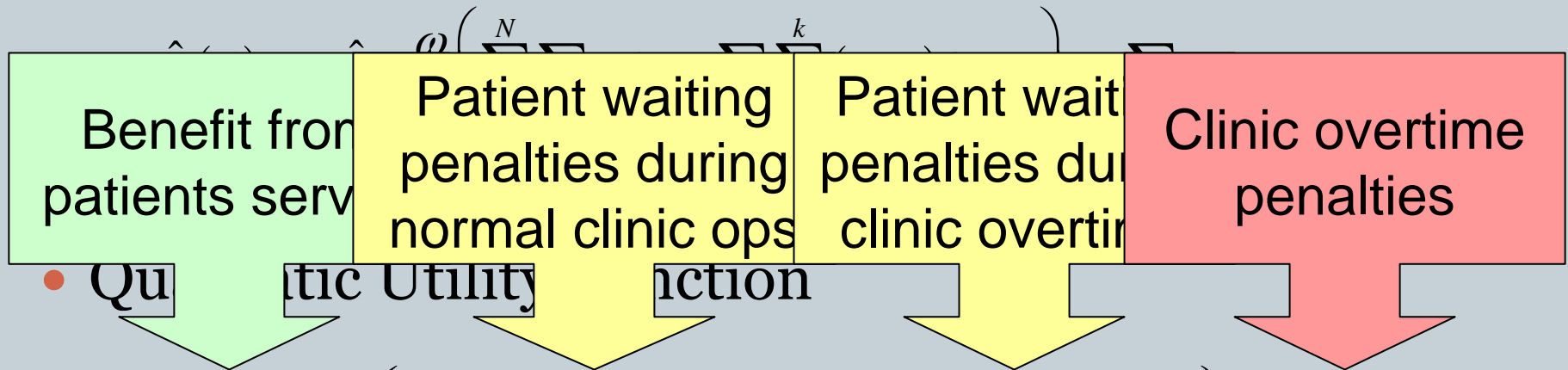
11

- $\pi$  = Benefit of seeing additional client
- $\omega$  = Penalty for client waiting
- $\tau$  = Penalty for clinic overtime
- Numéraire of  $\pi$ ,  $\omega$ , and  $\tau$  doesn't matter
  - Ratios (relative importance) are important
- Allow linear, quadratic, and mixed (linear + quadratic) costs

# Linear & Quadratic Objectives

12

- Linear Utility Function



$$\hat{U}(\mathbf{S}) = \pi \hat{A} - \frac{\omega}{\hat{A}} \left( \sum_{j=1}^N \sum_k (2k-1) \theta_{jk} + \sum_k \sum_{i=1}^k (i-1)^2 \theta_{N+1,k} \right) - \tau \sum_k k^2 \theta_{N+1,k}$$

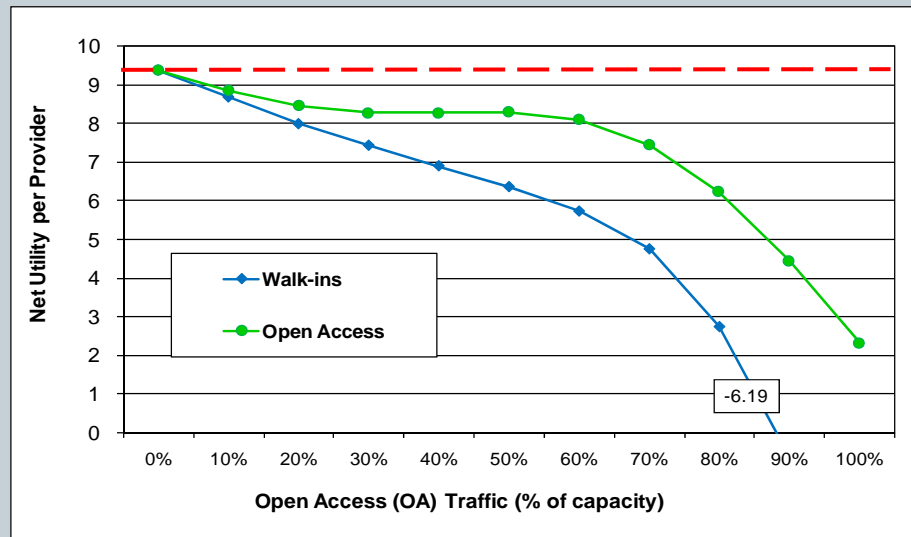
# Heuristic Solution Methodology

13

1. **Gradient search**
  - ✦ Increment/decrement appts scheduled in each slot
  - ✦ Choose the single change with greatest utility
  - ✦ Iterate until no further improvement found
2. **Pairwise interchange**
  - ✦ Exchange appts scheduled in all slot pairs
  - ✦ Choose the single swap with greatest utility
  - ✦ Iterate until no further improvement found
3. **Iterate (1) and (2) while utility improves**
4. **Prior research: Optimality not guaranteed, but almost always obtained**

# 3. Computational Results

14



# Computational Trials

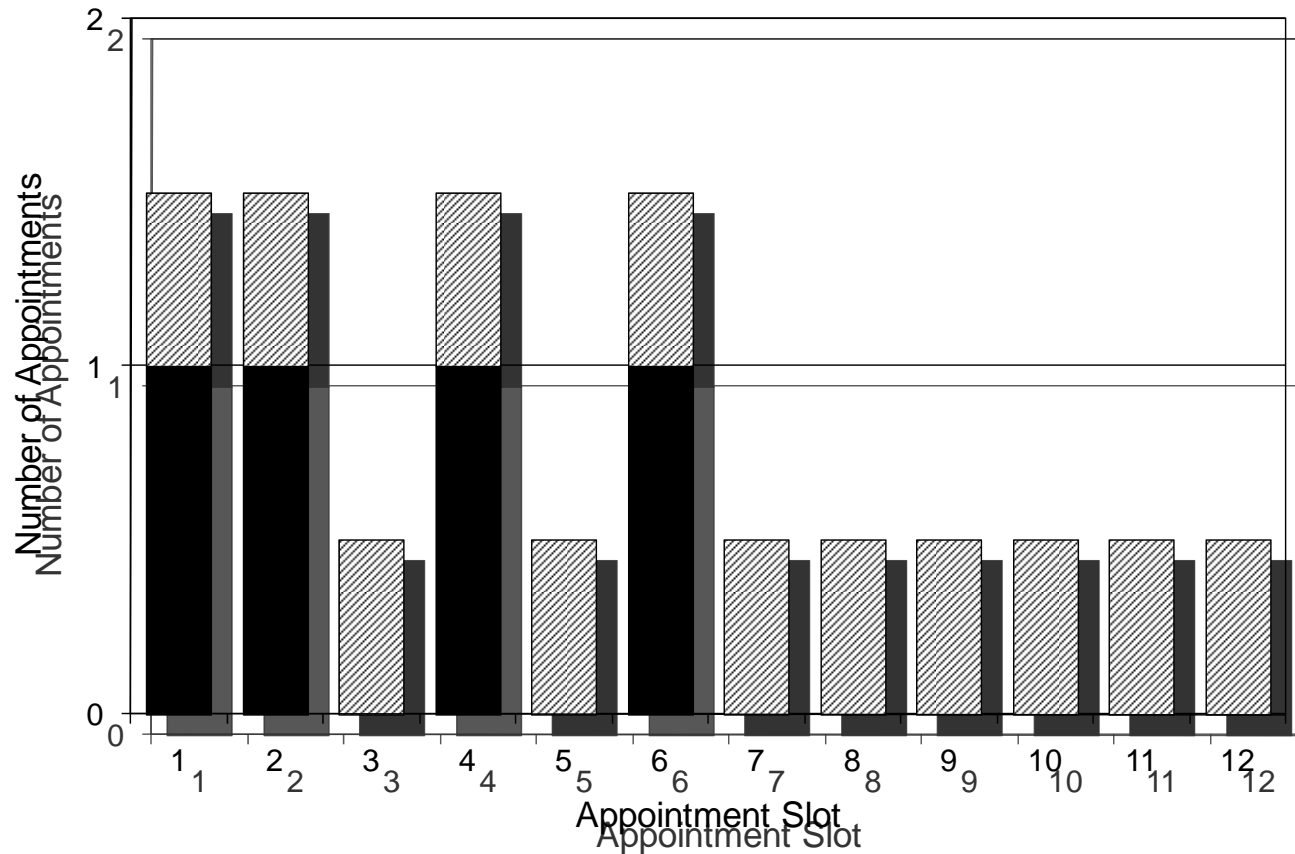
15

- 44 sample problems solved
- Session size  $N = 12$
- Appointment show rate  $\sigma = 70\%$
- Number of providers  $P = \{1, 2, 4, 8\}$
- OA call-in rate  $\lambda = \{0\%, 10\%, \dots 100\%\}$  capacity
  - With  $P = 4$  and  $N = 12$ , then  $\varphi = 24$  is 50% of capacity
- Walk-in rate  $\lambda = \{0\%, 10\%, \dots 100\%\}$  of capacity
  - With  $P = 4$ , then  $\lambda = 2$  is 50% of capacity
- Quadratic costs
  - Parameters  $\pi = 1.0$ ,  $\omega = 1.0$ ,  $\tau = 1.5$

# 50% Walk-Ins ( $\lambda = 0.5$ )

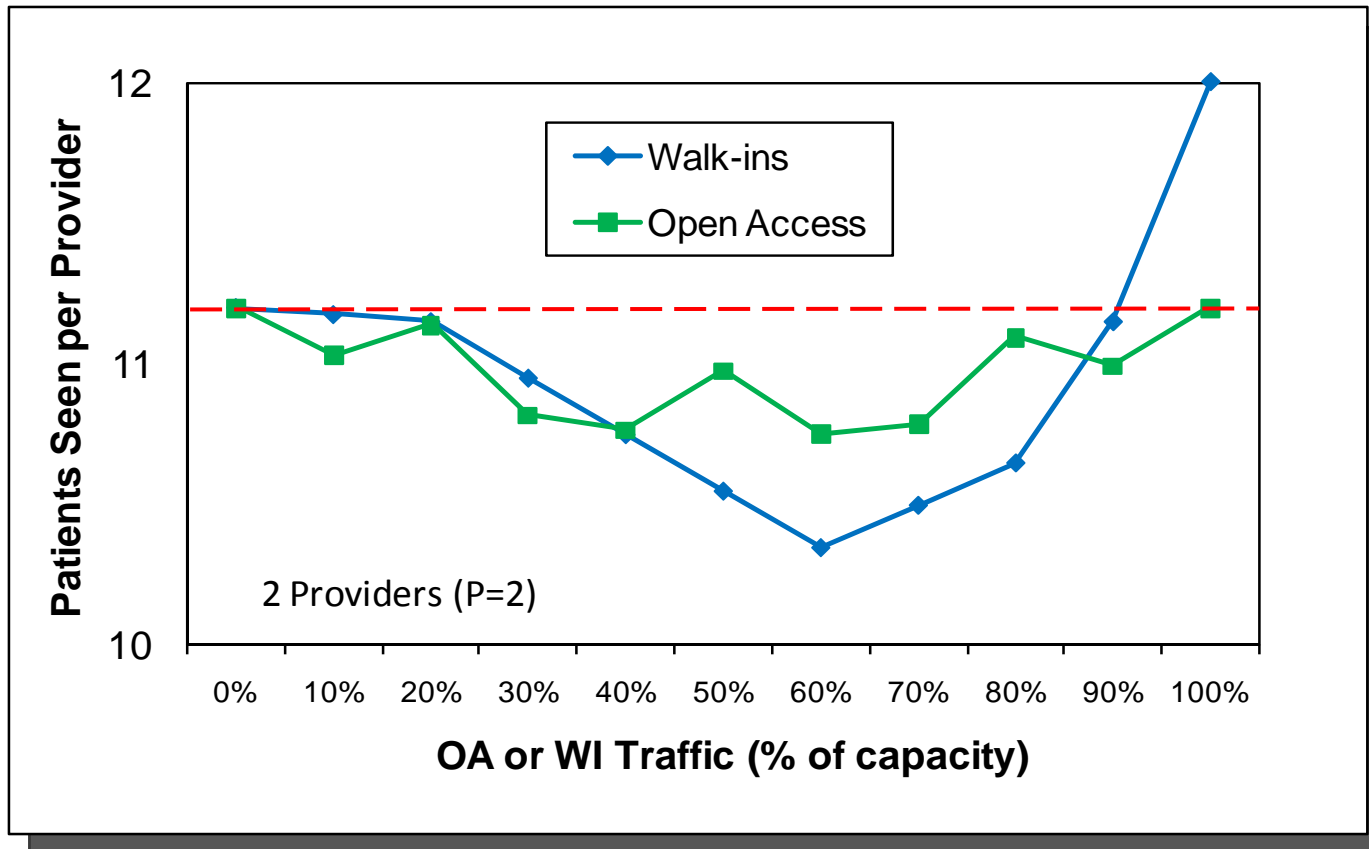
16

$N=12, P=1, \sigma=0.7, \pi=1.0, \omega=1.0, \tau=1.5$  (quadratic)



# Patients Seen

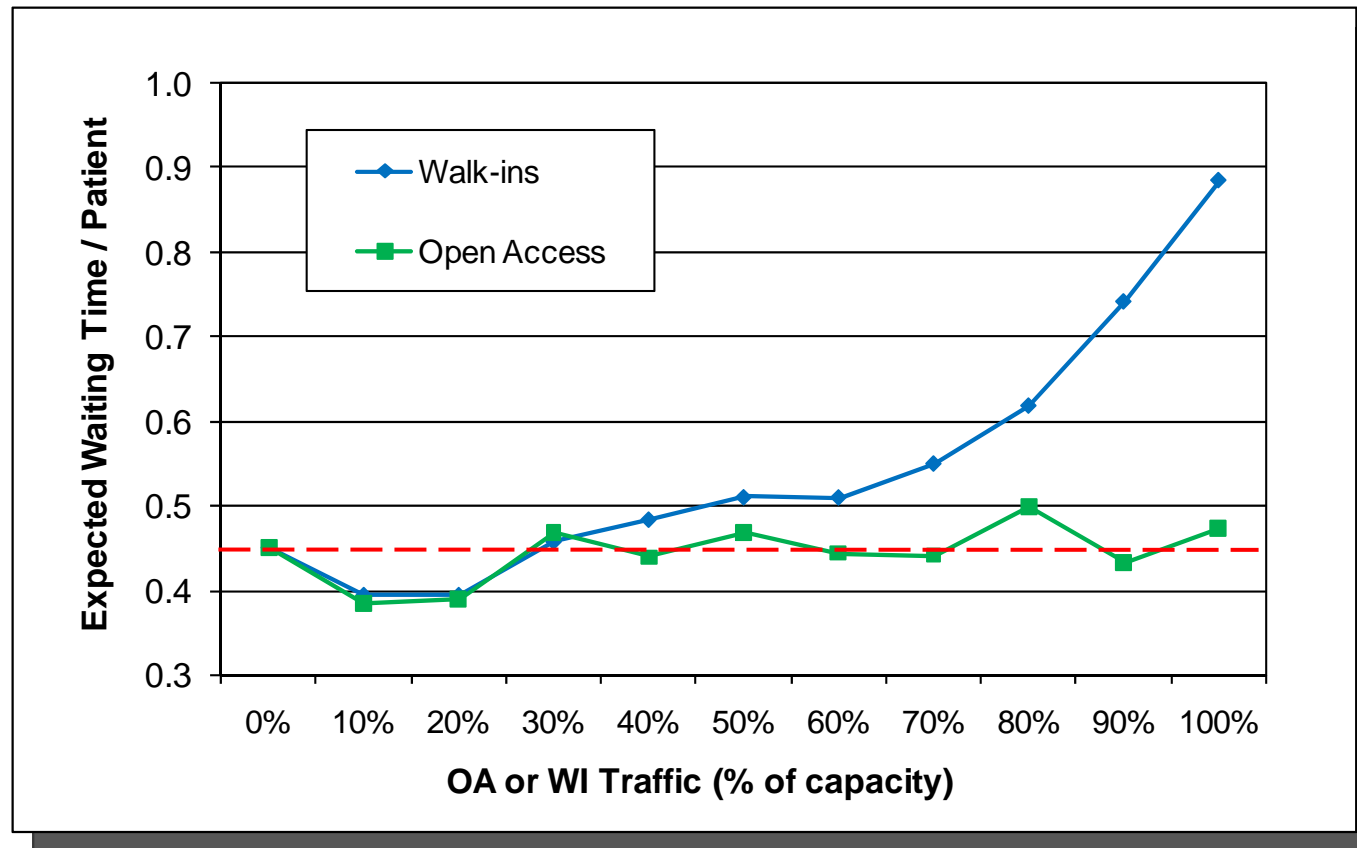
17



$N=12, P=1, \sigma=0.7, \pi=1.0, \alpha=1.0, \omega=1.0, \tau=1.5$

# Patient Waiting Time

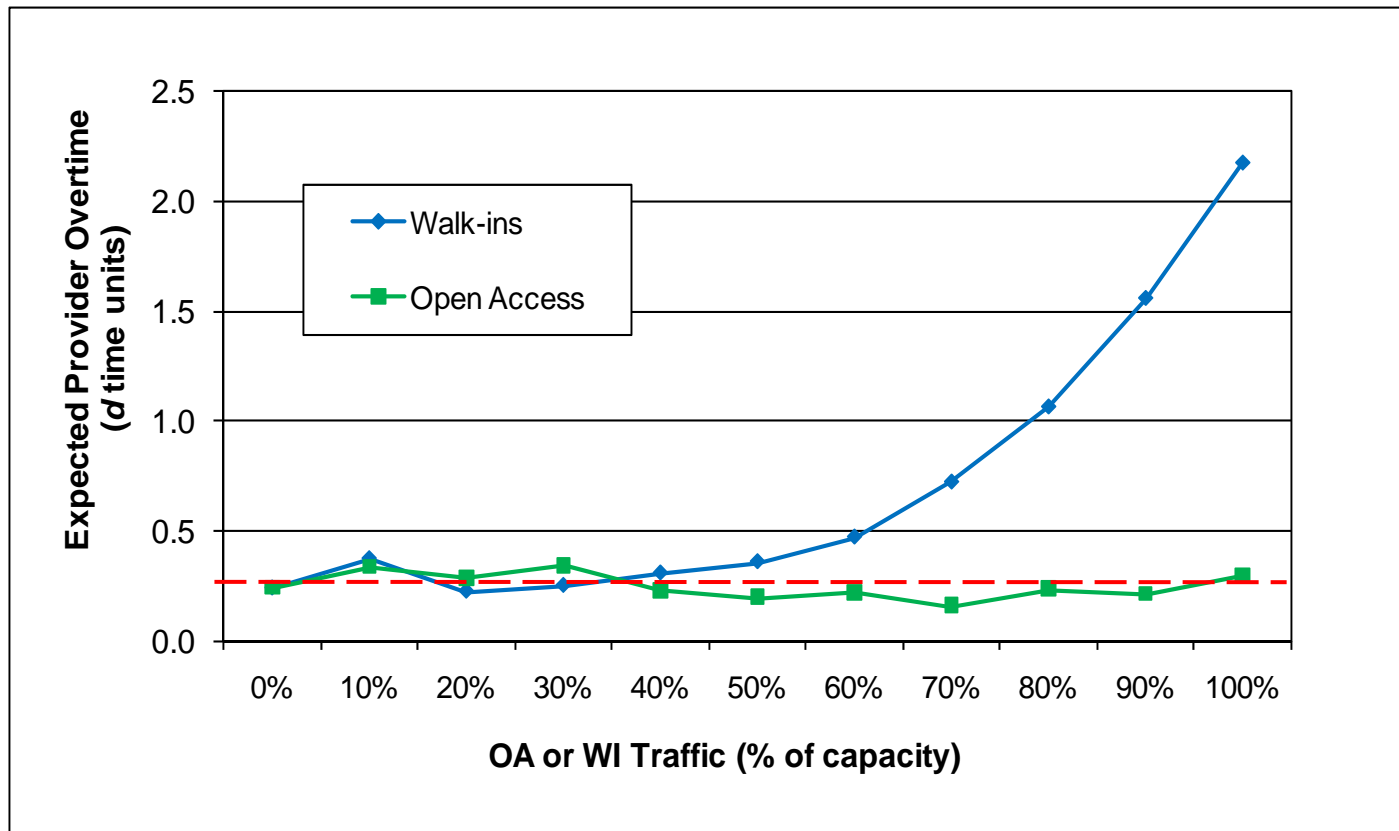
18



$N=12, P=1, \sigma=0.7, \pi=1.0, \alpha=1.0, \omega=1.0, \tau=1.5$

# Clinic Overtime

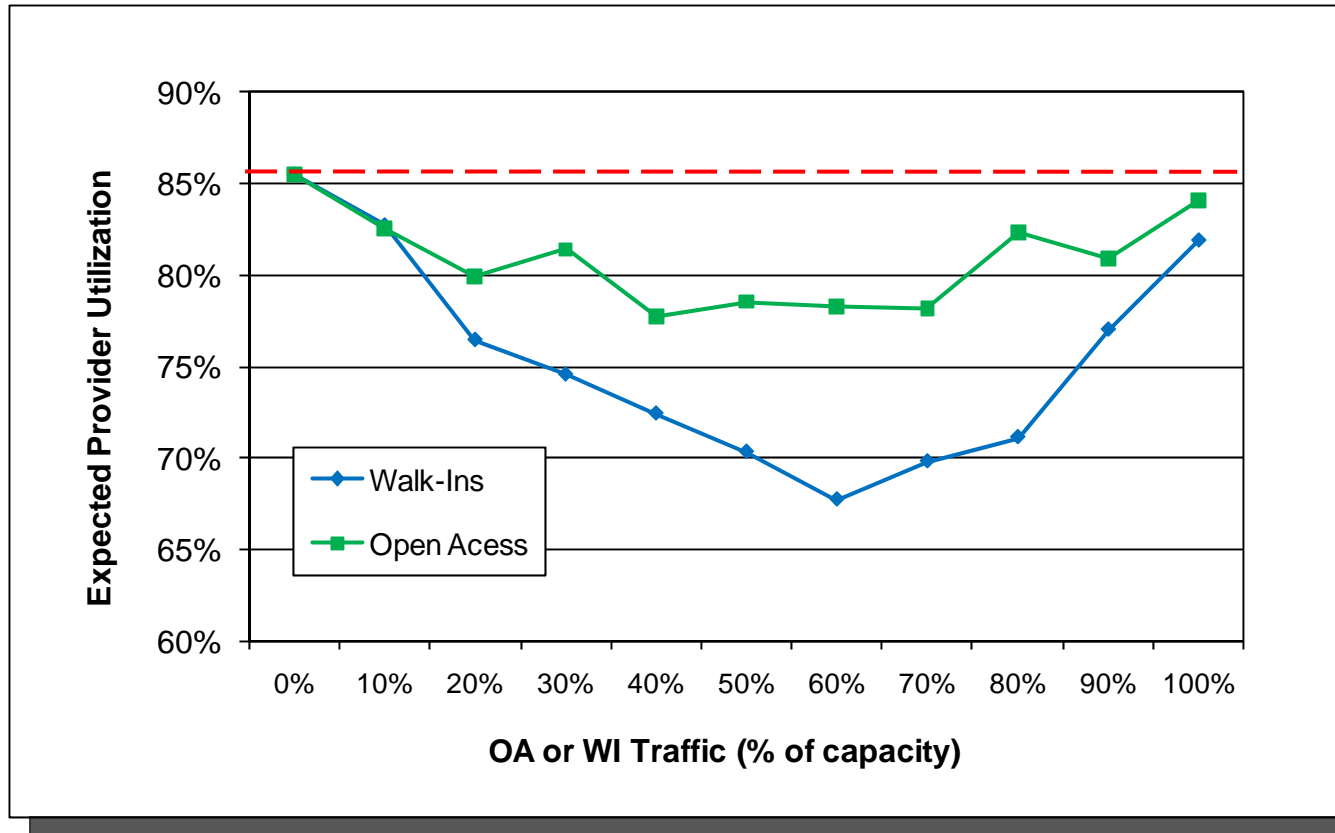
19



$N=12, P=1, \sigma=0.7, \pi=1.0, \alpha=1.0, \omega=1.0, \tau=1.5$

# Provider Utilization

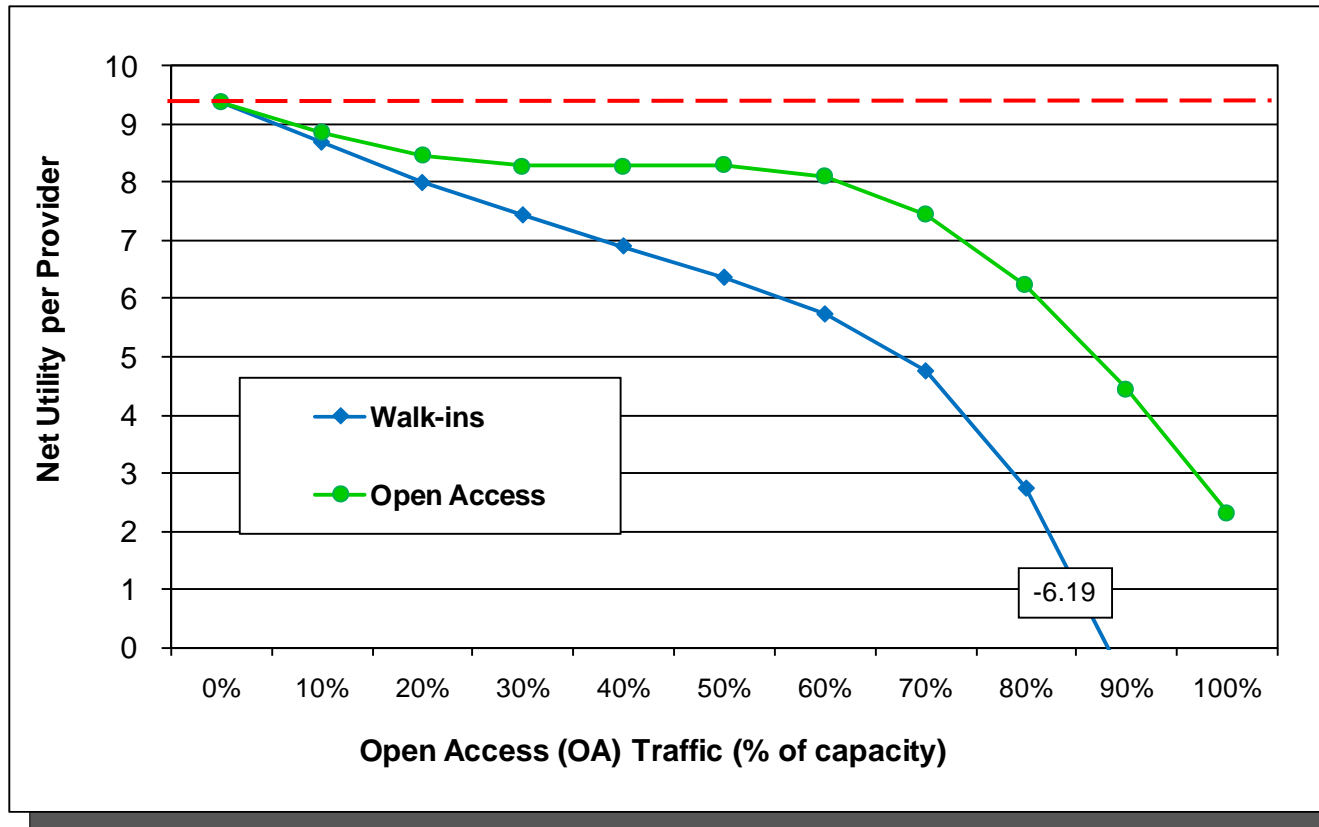
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$N=12, P=1, \sigma=0.7, \pi=1.0, \alpha=1.0, \omega=1.0, \tau=1.5$

# Net Utility

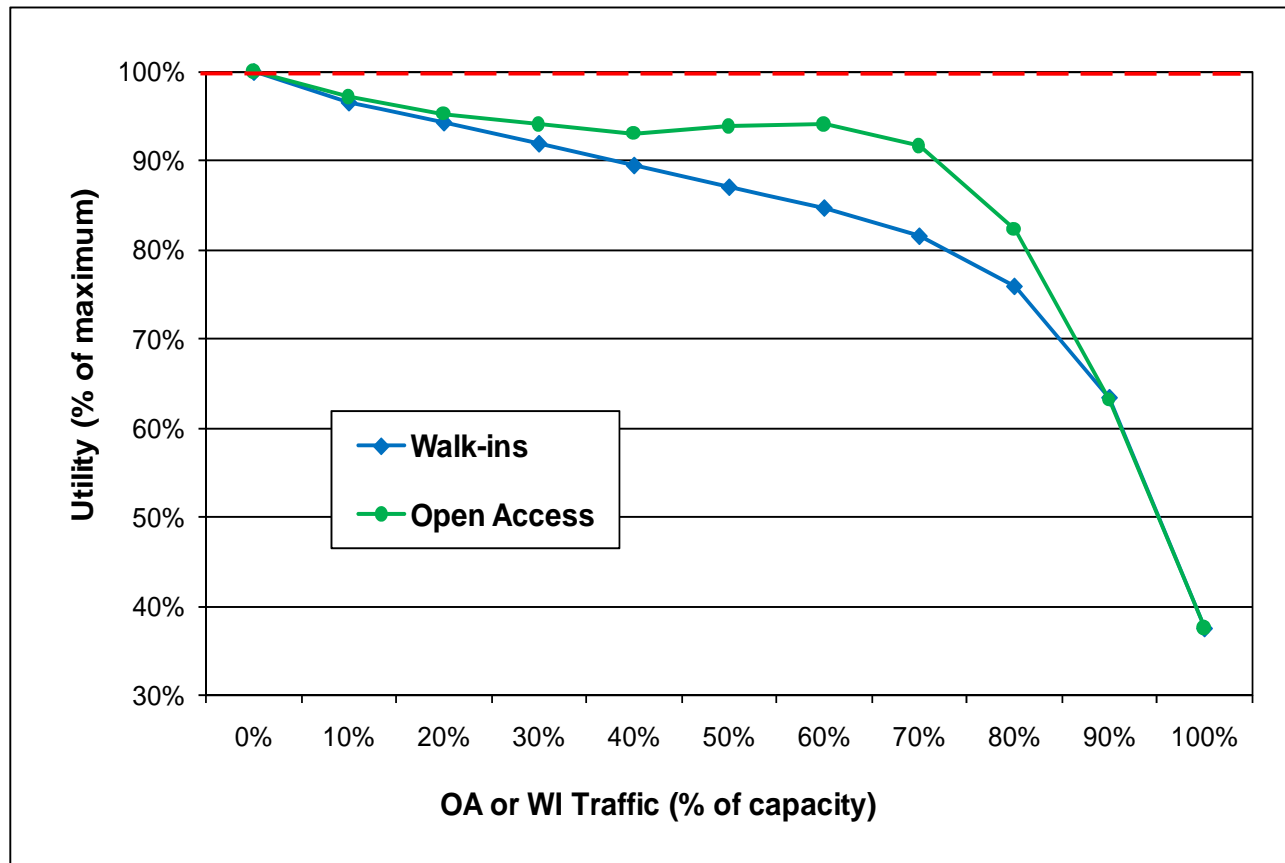
21



$N=12, P=1, \sigma=0.7, \pi=1.0, \alpha=1.0, \omega=1.0, \tau=1.5$

# % of Best Utility

22



$N=12, P=1, \sigma=0.7, \pi=1.0, \alpha=1.0, \omega=1.0, \tau=1.5$

# 4. Managerial Implications

23



# Managerial Implications

24

- TS appointments provide better clinic utility than does WI traffic or OA call-ins
  - Any WI or OA traffic causes some decline in utility
- An all-WI or all-OA clinic performs worse than any clinic with some TS appointments
  - Even a relatively small percentage of scheduled appointments can significantly improve clinic utility
  - Degree of improvement depends on number of providers
- A mix of TS appointments with some OA or WI traffic does not greatly reduce clinic performance (utility)

# Insights from the Model

25

- Loss of utility with WI traffic is due to the long right-tail of Poisson distribution
  - Excessive patient waiting & clinic overtime
- Loss of utility with OA traffic is due to uncertainty about number of OA call-ins
- TS appts reduce patient waiting and clinic overtime
  - Binomial distribution has truncated right tail
- Multiple providers improves clinic utility
  - Portfolio effect – variance reduction

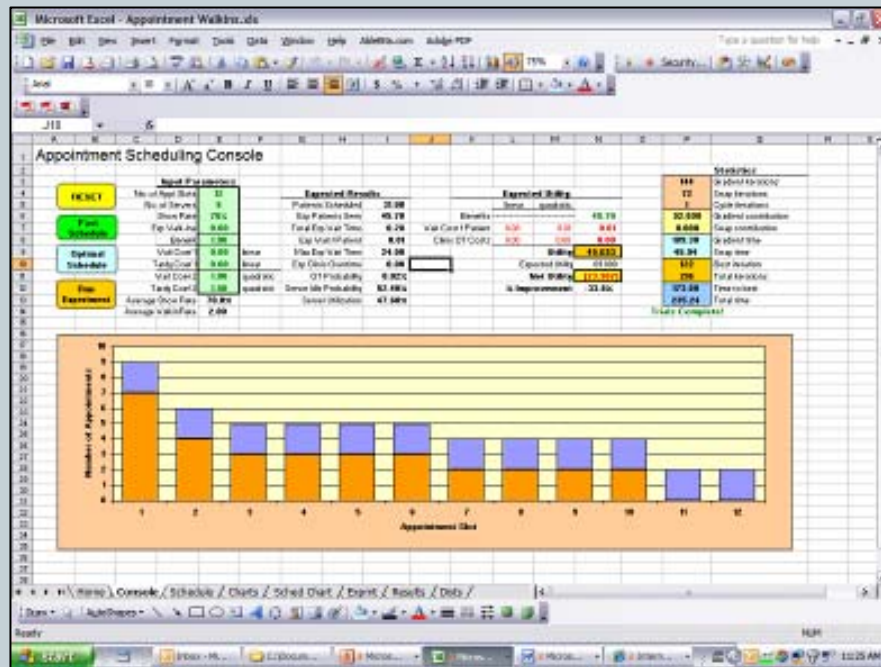
# Managerial Caveats

26

- Results (to date) are for “reasonable” utility parameters
  - Sensitivity analysis currently under way
- Attractiveness of WI and OA traffic may improve if they have a higher utility benefit than do scheduled appointments ( $\pi_{WI} > \pi_{TS}$ ;  $\pi_{OA} > \pi_{TS}$ )
  - Currently under investigation

# 5. Contributions & Future Research

27



# Contributions of Research

28

- Analytic yield management model for health care clinics with OA traffic
  - First to analytically examine combinations of TS and OA
- Fast and effective near-optimal solutions
- Demonstrate the trade-offs of OA traffic
  - Scheduled appointments provide higher utility
  - Even some appointments improve utility of an all OA clinic

# Future Work

29

- **Determine sensitivity of results**
  - Utility parameters, number of slots, show rates, linear costs
  - Show rates, walk-in rates, and providers vary by time of day
- **Extend model**
  - Different utility parameters for appointments and walk-ins
  - Walk-ins seen before appointments and vice versa
  - Stochastic service times

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30

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